

B.B.M. COLLEGE, BALIAPUR, DHANBAD

Internal Exam – 2024

SEMESTER – I to IV

Special Exam

Class – B.Sc. (Math)
Sub. – GE Paper -II

Time –
F.M. – 20 each Sem.

SEMESTER – I

Answer any two question

Time – 1 Hr

F.M. - 20

- (1) state and prove Leibnitz's theorem
- (2) using E-d definition , prove that the function

$$F(x) = \int x^2 \sin \frac{1}{x} \text{ if } x \neq 0$$

0 , if $x = 0$

Is continuous at $x=0$.

- (3) if $(\tan^{-1}x)^2$, prove that

$$(1+x^2) \frac{d^2y}{dx^2} + 2x(1+x^2) \frac{dy}{dx} = 2 .$$

- (4) Evaluate the integral $\int_0^{\frac{\pi}{2}} \sin^n x dx$.

- (5) if $v = x^2yz \mathbf{i} + xy^2z \mathbf{j} + xyz^2 \mathbf{k}$

SEMESTER – II

Answer any two question

Time – 1 Hr

F.M. - 20

- (1) solve : $\frac{dy}{dx} = e^{x+y} + x^2 e^y$.

- (2) solve : $\frac{dy}{dx} + 1 = e^{x-y}$.

- (3) solve : $\frac{dy}{dx} = \frac{x^2+y^2}{2x^2}$.

- (4) solve : $p^2 - 7p + 12 = 0$.

- (5) solve by carpet's method

$$(p^2 + q^2) y = qz .$$

SEMESTER – III

Answer any two question

Time – 1 Hr

F.M. - 20

- (1) define countable and uncountable sets.
- (2) state and prove Bolzano – weierstrass theorem for sequoias .
- (3) test the series converge or diverge whose general term is

$$U_n = \sqrt{n^4 + 1} - \sqrt{n^4 + 1} .$$

- (4) prove that the series

$$\frac{1}{1^p} + \frac{1}{2^p} + \frac{1}{3^p} + \dots + \frac{1}{n^p} \dots \text{ is convergent if } P > 1 \text{ and divergent if } P \leq 1 .$$

- (5) state and prove robe's test

Or

State and prove Cauchy root test .

SEMESTER – IV

Answer any two question

Time – 1 Hr

F.M. - 20

- (1) define a group with example .
- (2) state and prove Lagrange's theorem .
- (3) define normal subgroups .
- (4) define a ring with examples .
- (5) prove that every finite integral domain is a field .